

# Math Diversion Problem 656

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Learning is a treasure that will follow its owner everywhere.  
— Chinese proverb

The problem is found at:

Source: Finite Mathematics, 5th Ed. Brooks/Cole  
(2002), p. 57  
Title: A Mixed-rate problem  
Presenter: H. Rolf

## 1 The Problem

A woman must control her diet. She selects milk and bagel for breakfast. How much of each should she serve in order to consume 700 calories and 28 grams of protein? Each cup of milk contains 170 calories and 8 grams of protein. Each bagel contains 138 calories and 4 grams of protein.

SOLUTION:

### Conceptualizing the problem

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Calories per unit:	170/cup		138/bagel				
Protein (gm) / unit:	8/cup		4/bagel				
Description:	<table border="1"><tr><td>Milk</td></tr></table>	Milk	+	<table border="1"><tr><td>Bagel</td></tr></table>	Bagel	→ <table border="1"><tr><td>Complete meal</td></tr></table>	Complete meal
Milk							
Bagel							
Complete meal							
Quantities:	$x$		$y$	Total calories = 700 Total grams protein = 28			

Figure 1. As usual, rates are placed above and quantities (and totals) are placed below. (Units:  $x$  is in cups and  $y$  is in whole bagels.)

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We simply have two totals to deal with, employing the given constraints on the amounts of each. Referencing Figure 1, we have that (balancing first for calories

and then for protein)

$$170x + 138y = 700, \quad (1a)$$

$$8x + 4y = 28, \quad (1b)$$

which has solution

$$x = \frac{133}{53} \approx 2.5 \quad \text{and} \quad y = \frac{105}{53} \approx 2. \quad (2)$$

That is, the meal is to consist of 2.5 cups of milk and 2 bagels.