

Math Diversion Problem 888

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I take the positivist viewpoint that a physical theory is just a mathematical model and that it is meaningless to ask whether it corresponds to reality. All that one can ask is that its predictions should be in agreement with observation. — Stephen Hawking
[*The Nature of Space and Time*, p.3–4]

Source: <http://regentsprep.org/Regents/math/ALGEBRA/AE3/PracWo>
Title: Cups in Pitchers
Presenter: Patrick

1 Problem

Two small pitchers and one large pitcher can hold 8 cups of water. One large pitcher minus one small pitcher constitutes 2 cups of water. How many cups of water can each pitcher hold?

2 Solution

Rate of holding cups of water per pitcher:	R_S		R_L		
Pitcher size:	Small	+	Large	→	Comb. pitchers
Substitution vars:	x		y		Total cups available
Combination #1:	2		1	→	8
Combination #2:	-1		1	→	2

Figure 1. Standard setup for calculation: $R_Sx + R_Ly = \text{Total cups}$.

We can easily glean from Figure 1 the information to write the coupled equations

$$\begin{aligned}(2)R_S + (1)R_L &= 8, \\ (-1)R_S + (1)R_L &= 2,\end{aligned}\tag{1}$$

which as solution $R_S = 2$ cups per small pitcher, and $R_L = 4$ cups per large pitcher.