

# Math Diversion 1078

P. Reany

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We must use time as a tool, not as a couch.

— John F. Kennedy

Source: <https://answers.yahoo.com/question/index?qid=20080214222603AAcQyvt>

Title: A Mixed-Rate Problem

Presenter: Patrick

## 1 Problem

An employer has a daily payroll of \$1950 when employing some workers at \$120 per day [type B worker] and others at \$150 per day [type A worker]. When the number of \$120 workers is increased by 50% and the number of \$150 workers is decreased by  $1/5$ , the new daily payroll is \$2,400. Find how many workers were originally employed at each rate.

## 2 Solution

This is a fairly simple mixed-rate problem. Let's start with a figure.

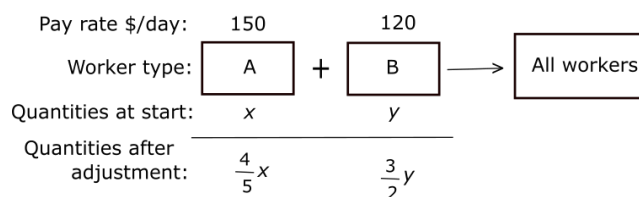


Figure 3. Standard mixed-rate problem. To increase by 50% is to multiply by  $3/2$ . To decrease by a  $1/5$ th is to leave  $4/5$ th.

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For each configuration of workers, we have a distinct 'total as the sum of its parts' to write down:

$$150x + 120y = 1950, \tag{1a}$$

and

$$150\left(\frac{4}{5}x\right) + 120\left(\frac{3}{2}y\right) = 2400. \quad (1b)$$

The solution to this system is  $x = 5$  and  $y = 10$ .