## Math Diversion Problem 71

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Mathematics is the science of the infinite.

— Augustin-Louis Cauchy

The YouTube video is found at:

Source: https://www.youtube.com/watch?v=lfxCDP7y\_D8
Title:A tricky Solution from Stanford University
Admission Interview
Presenter: Super Academy

1 The Problem

Given the relation

$$K^2 = 8i, (1)$$

find the values of K.

## 2 The Solution

First, let's rearrange (1) to get

$$K^2 = 8e^{\pi i/2} \,. \tag{2}$$

Therefore,

$$K = \pm \sqrt{8} (e^{\pi i/2})^{1/2}$$

$$= \pm 2\sqrt{2} e^{\pi i/4}$$

$$= \pm 2\sqrt{2} \frac{1}{\sqrt{2}} (1+i)$$

$$= \pm 2(1+i). \tag{3}$$